1.0

1.1

1.25

2.8   2.5
3.2   2.2
3.6
4.0   2.0

1.4   1.6

1.8

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Technical Report No. 28

TR-28

A PROCEDURE FOR EVALUATING FRACTURE DYNAMIC PARAMETERS

FROM CRACK VELOCITY MEASUREMENTS

by

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May 1977

16 p.

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A PROCEDURE FOR EVALUATING FRACTURE DYNAMIC PARAMETERS FROM CRACK VELOCITY MEASUREMENTS

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ABSTRACT

A combined numerical and experimental procedure for evaluating some of the fracture dynamic parameters which govern the crack run-arrest response in a fracturing plate are discussed. A dynamic finite element code is used to compute the dynamic stress intensity factor and dynamic energy release rate associated with a propagating crack which is driven by the experimentally determined crack velocity. Numerical results generated by the developed procedure are then compared with dynamic stress intensity factors obtained through dynamic photoelastic analyses of fracturing Homalite-100 plates. Two edge-cracked specimens with fixed edge displacement loadings and two wedge-loaded double cantilever beam specimens were considered in this comparative study. Good agreements were obtained between the results obtained by the developed numerical-experimental procedure and dynamic photoelasticity.

INTRODUCTION

The three approaches currently in use in fracture dynamic studies are: to relate the experimentally determined crack velocities with static fracture parameters [1]; to relate experimentally determined crack velocities with those obtained from an analytical dynamic model without or with postulated dynamic fracture toughness [2,3,4]; and to determine experimentally the dynamic state of stress in fracturing polymeric materials [5,6,7]. In this paper, a fourth procedure, which utilizes the versatility of dynamic finite element method (FEM) to extract fracture dynamic parameters from the most commonly measured quantity of crack velocity in practical structural material is described. The procedure is then used to indicate the errors involved in using static analysis to interpret dynamic results.

DYNAMIC FINITE ELEMENT CODE

The dynamic finite element method (FEM) which has evolved since its initial use [8] in this combined numerical-experimental procedure is the FEM

code HONDO [9] with artificial viscosity to reduce the keystoning effect in the finite elements along the opening crack surfaces. In this dynamic FEM procedure, crack extension is modeled by discontinuous jumps of the crack tip from one finite element node to its adjacent node and the time-averaged crack tip displacement is equated to the average crack tip velocity at the adjacent node. The average work necessary to open the newly created increment of crack surface is then used to compute the surface energy dissipation rate which is equated to the dynamic energy release rate at the crack tip node just prior to the subsequent discrete movement of the crack tip [8]. An accuracy check of this direct procedure for computing the dynamic energy release rate was established by a comparative study with Baker's solution [10] where the numerical and theoretical results agreed within 1 percent of each other [8].

More recently another check on the dynamic finite element algorithm was made by comparing the crack opening displacements (COD) of a constant velocity crack against the theoretical solution of Broberg [11]. In this numerical study involving a fracturing steel plate, an artificial keystone viscosity of B3=0.2 was used to damp out the keystoning effect prevalent in previous analyses. The numerically determined time-averaged COD at every other node away from the moving crack tip was found to be in excellent agreement with Broberg's result for a crack velocity of $c/c_1 = 0.076$ where c and c_1 are the crack and dilatational wave velocities, respectively [12]. It was also shown that at this low crack velocity, the stress intensity factor computed by static near field solution was only 2.2 percent higher than that computed by the dynamic near field solution when dynamic finite element COD values were used to compute the dynamic stress intensity factor.

In order to examine further the effectiveness of the above COD technique in dynamic finite element analysis of fracturing Homalite-100 plates, the well analyzed fracturing dynamic photoelastic specimens B2 and B13 [8] were reanalyzed with various artificial viscosities. The finite element breakdown and the crack velocities used in this new study are identical to those used in Reference [8]. Figure 1 shows the crack opening displacements at three crack lengths in Specimen B2 with three artificial viscosities. The small artificial viscosity of B3 = 0.01 and 0.1 were not very effective in removing keystoning but the prominent fluctuations in COD were substantially suppressed with B3 = 0.5. It should also be noted that a significant change was made in the numerical algorithm where the initial residual surface tractions along crack propagation were computed by using a static modulus of elasticity of E_S = 540 ksi while all stress wave propagation induced by the running crack were computed with a dynamic modulus of elasticity of E_D = 675 ksi. This combined use of static and dynamic moduli of elasticity in dynamic finite element analysis, initially proposed by Gehlen [13], is an attempt to model the strain rate sensitivity of the modulus of elasticity of Homalite-100 material. Such strain rate sensitivity did not exist in the fracture dynamic analysis of steel tapered DCB specimen [12] which is easier to analyze by dynamic finite element analysis than the photoelastic specimens. Our continuing interest in using dynamic photoelasticity to study fracture dynamics despite the added complexity of strain rate sensitivity
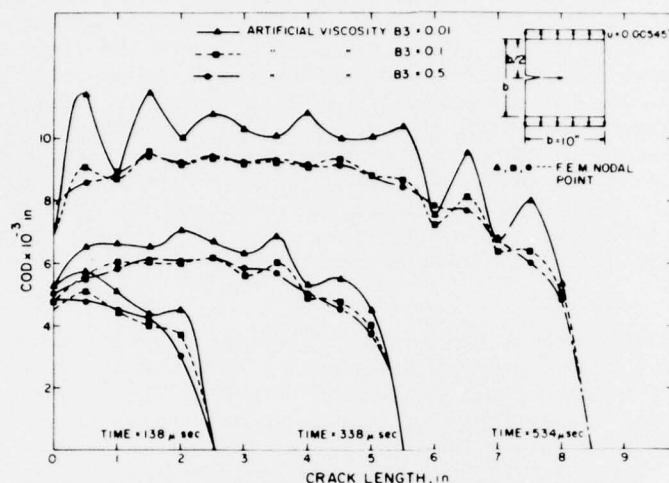
Fig. (1) - Effect of artificial keystone viscosity on COD in
Test No. B2.

stems from the fact that no other experimental technique can provide an ac-
curate near field state of stress in the vicinity of a running crack. Dy-
namic photoelasticity is one of few optical techniques which can provide
experimentally determined dynamic stress intensity factor with which our
numerical results could be compared. As will be shown later, such dynamic
stress intensity factors computed through the combined use of static and
dynamic moduli of elasticity agreed well with the experimental results under
the state of plane strain.   The latter state of plane strain for thicker
Homalite-100 plates is considered to be a better modeling of the cleavage
fractured surface observed in the fractured specimens.

Figure 2 shows the variations in dynamic stress intensity factors ob-
tained numerically by the energy release rate method [8] and COD method [12]
as well as their experimental counterpart determined by dynamic photoelas-
ticity for Specimen B2. While the two numerical algorithms of computing
dynamic stress intensity factors do not yield substantially different re-
sults, the more pronounced fluctuation in dynamic stress intensity factors
computed by the COD method is noted. Thus this comparison favors the ener-
gy release rate procedure.

Likewise comparison is shown in Figure 3 for Specimen B13 in which the
crack arrested. While the prominent peak in the experimentally determined
dynamic stress intensity factor was not observed in the two numerical values,
the experimental and numerical results are otherwise in good agreement with
each other. Again the numerical results obtained by energy release rate
procedure appears to be in slightly better agreement with the experimental
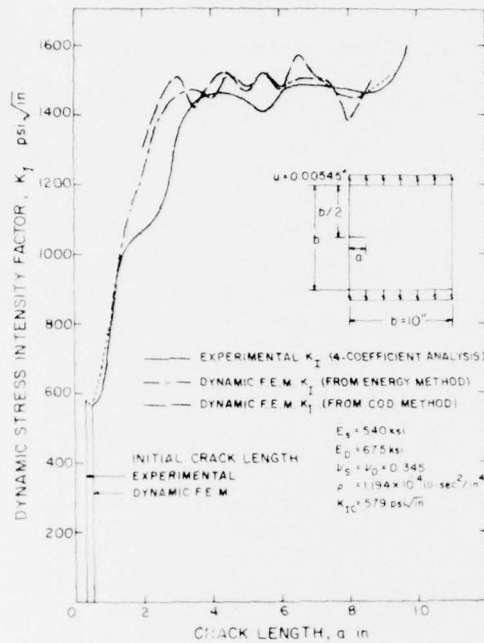results.

Fig. (2) – Dynamic stress inten-
sity factors in Test
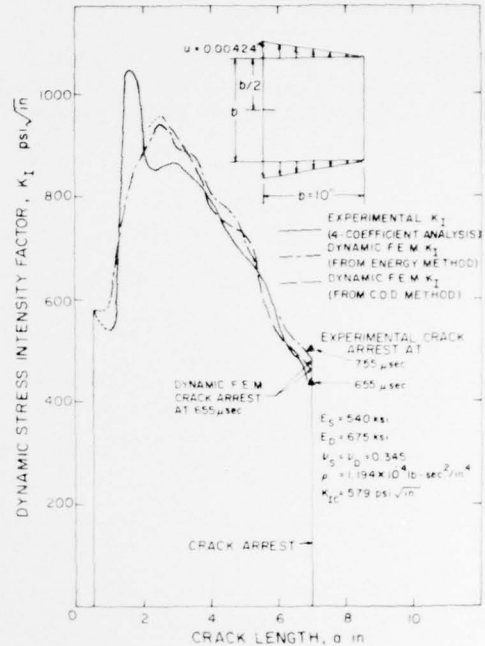No. B2, plane strain
analysis

Fig. (3) – Dynamic stress inten-
sity factors in Test
No. B13, plane strain
analysis

As a result of these two comparative studies using the well analyzed specimens B2 and B13, it was concluded that the energy release rate procedure provided slightly better numerical results of the fracturing Homalite-100 plates. This conclusion unfortunately differs with that in Reference [12] and is perhaps indicative of the larger keystoning effect in the Homalite-100 plates due to its much smaller modulus of elasticity.

WEDGE-LOADED DCB SPECIMEN

The above dynamic finite element algorithm was then used to analyze the dynamic crack arrest results of two wedge-loaded double cantilever beam (DCB) specimens machined from Homalite-100 plates of 1/2 inch nominal thickness [14]. The dynamic stress intensity factors of these two fracturing tapered DCB specimens were determined by a different data reduction scheme of dynamic photoelasticity results than that used by the authors [7]. The static and dynamic material properties as well as the crack position versus time relations reported in Reference [14] were used as input conditions to

our dynamic finite element analysis.

Figure 4 shows the finite element breakdown of one of the two tapered DCB specimens. Figures 5(a) and (b) show the crack position versus time relations which were used to propagate the crack tip intermittently along
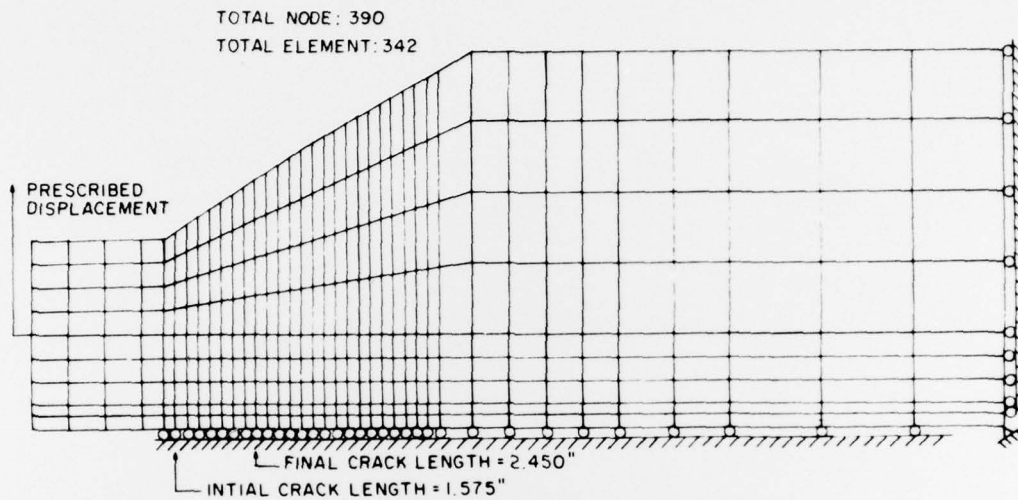
TOTAL NODE: 390
TOTAL ELEMENT: 342

Fig. (4) - Finite element breakdown of wedge-loaded C-DCB
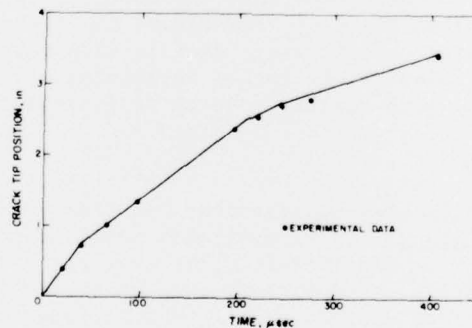model No. 7 [14]

Fig. 5(a) - Crack tip position versus time in C-DCB model
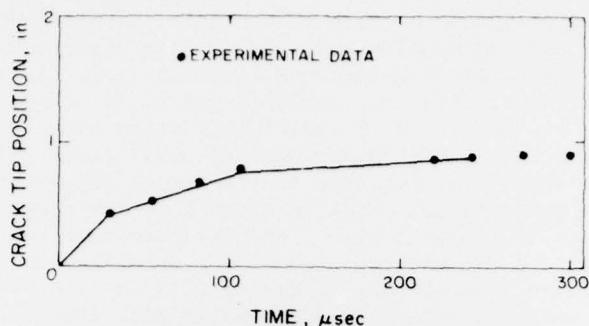No. 6 [14]

Fig. 5(b) - Crack tip position versus time in C-DCB model
No. 7 [14]

the finite element nodes at prescribed time intervals. Fixed pin displacements were prescribed during the entire fracture process which were 459 and 300 microseconds for Specimens C-DCB Model Nos. 6 and 7, respectively. This assumption of fixed grip condition has been the source of discussion since one of the authors presented a dynamic finite element analysis of the crack propagation and arrest in a tapered DCB specimen using measured crack velocities [15]. The static stress intensity factor at crack arrest computed under the assumption of fixed grip condition was approximately 40 percent lower than the corresponding value computed under the assumption of variable load condition of Reference [16], thus indicating the sensitivity of the arrest stress intensity factor to the prescribed boundary condition during crack propagation in such small crack arrest specimen. Subsequent analysis of another tapered DCB specimen under the two different loading conditions of our fixed grip loading and the variable loading condition prescribed in References [16] and [17] showed that while the dynamic strains computed under the former condition agreed well with the three strain gage measurements [16], the corresponding dynamic strains computed under the assumption of variable loading differed considerably with experimental results [12]. As a result of this analysis [12], the fixed grip condition is believed to be a valid assumption in the series of experiments reported in Reference [16]. This conclusion also indicates that the crack arrest stress intensity factor determined by the procedure described in References [16] and [17] could grossly overestimate the crack arrest potential of the material tested.

Unfortunately, the excellent agreements between the crack arrest stress intensity factors determined by simulations of the crack arrest experiments of References [16] and [17] using Homalite-100 specimens [14] and the crack arrest stress intensity factors determined independently by dynamic photoelasticity [5] have been used as experimental evidence for justifying the variable pin loading in References [16] and [17]. A cursory study, however,

shows considerable differences between the relative compliances between the loading fixture and the Homalite-100 specimen in the dynamic photoelasticity experiments and those of References [16] and [17]. As a result, one can conclude qualitatively that the variable pin loads measured in the rigid loading fixture of the simulated experiments using Homalite-100 specimens should be closer to the pin loads obtained under fixed grip condition while such condition cannot be realized in the actual experiments using steel specimen. An experimental check in these relative compliances can be easily made to verify such hypothesis. Another procedure is to analyze numerically the fracture dynamic response of the Homalite-100 specimens following the procedure described in Reference [15] and then identify the differences or similarities between these results with those of Reference [12]. Dynamic finite element analyses under the fixed grip condition should thus provide this insight into the controversy surrounding the exact boundary conditions on the tapered DCB specimens used in crack arrest experiments.

Figure 6 shows the dynamic and static stress intensity factors obtained by static and dynamic finite element analyses under the assumption of fixed grip condition for a Homalite-100 C-DCB Model No. 6 [14]. Also shown are
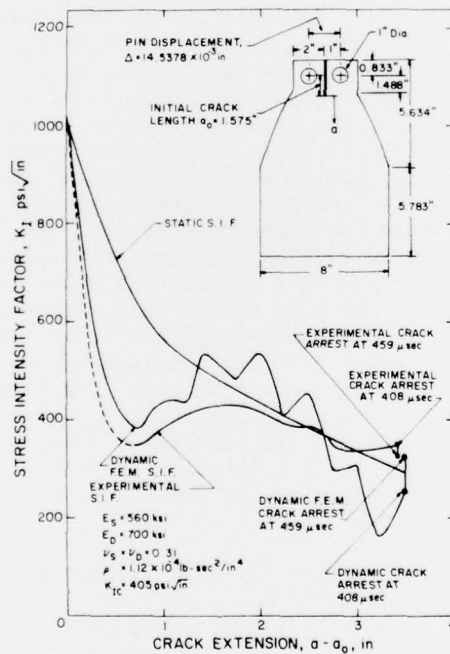

Fig. (6) - Stress intensity factors in a wedge-loaded contoured DCB specimen (Model No. 6). Load at fracture initiation = 151 lb [14].

the dynamic stress intensity factors of this specimen obtained by dynamic photoelasticity [14]. While the numerically obtained dynamic stress intensity factors show some small oscillations, the two results are generally in qualitative agreement with each other and in particular are in excellent agreement at crack arrest.

Figure 7 shows the crack opening displacements (COD) of the same specimen. As expected, the keystoning effect continues to increase with
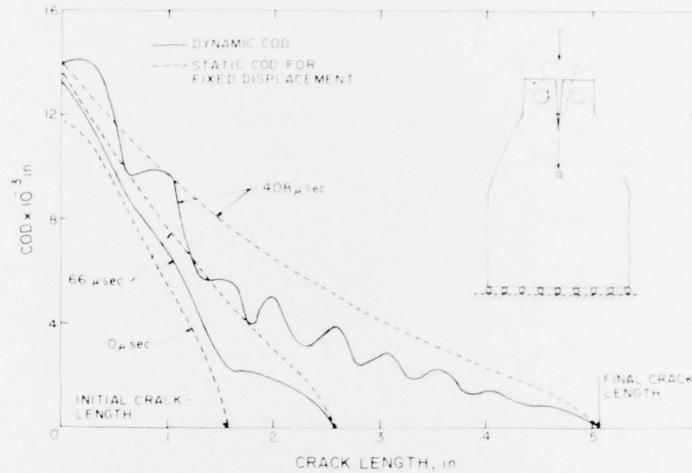
Fig. (7) - Crack opening displacement (COD) at different times in C-DCB Model No. 6 [14]

increase in crack length despite the high artificial viscosity of B3 = 0.5. The pronounced smaller dynamic crack opening displacements, which was also observed in the metallic specimens [12,15], in this cantilever beam type specimen are indications of the delayed response of the propagating crack tip to the applied load at the loading pin. Such delay response further verifies our assumed fixed grip loading condition during crack propagation and arrest.

Figure 8 shows the dynamic and static stress intensity factors in Specimen C-DCB Model No. 7. Again, relatively good agreement, particularly at crack arrest, between the experimental and numerical results is noted. The rapid small oscillations in dynamic stress intensity factors, which were noted in Figure 6, are absent in Figure 8. Our past experiences in numerical fracture dynamic analyses [4, 12] indicate that smoothed crack velocities generally result in oscillations in dynamic stress intensity factors and vice versa. Since the test results of Model C-DCB No. 6 recorded 9 crack positions for a crack extension of 3.41 in. while 7 crack positions are
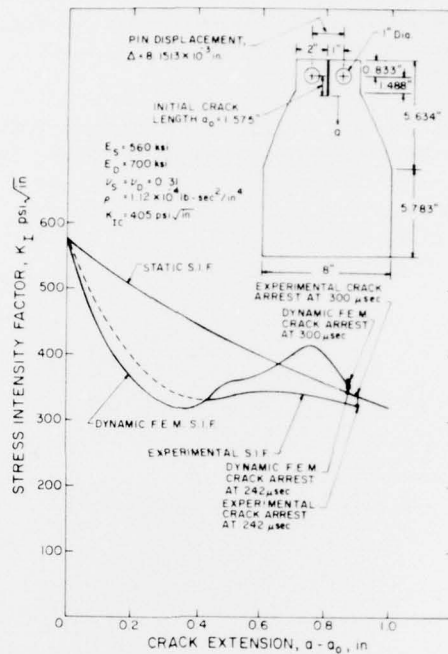
Fig. (8) - Stress intensity factors in a wedge-loaded contoured
        DCB specimen (Model No. 7). Load at fracture initia-
        tion = 89 lb [14].

recorded for a crack extension of 0.90 in. for Model 7, one would expect the
crack position versus time relation for the test of Model 6 to represent a
smoother time average position instead of a more precise crack position ver-
sus time relation necessary to generate a smoothly varying dynamic stress
intensity as was the case of Model No. 7 test. Thus Model No. 7 should
yield smoother variations in numerically computed dynamic stress intensity
factor than Model No. 6.

The above good agreement between the variations in dynamic stress inten-
sity factors with crack propagation obtained numerically and experimentally
verifies the validity of the fixed grip condition under which the dynamic
stress intensity factors were computed. Although the numerical results pro-
vide the variations in pin loads with respect to crack propagation as shown
in Figure 9, corresponding experimental results were not available for
direct comparison. Thus experimentally measured pin load from a separate
test [14] is shown in Figure 9 for qualitative comparison. The two-fold
differences between ringing frequencies of the numerical and experimental
pin loads could be due to unavoidable compliance of the loading frame and
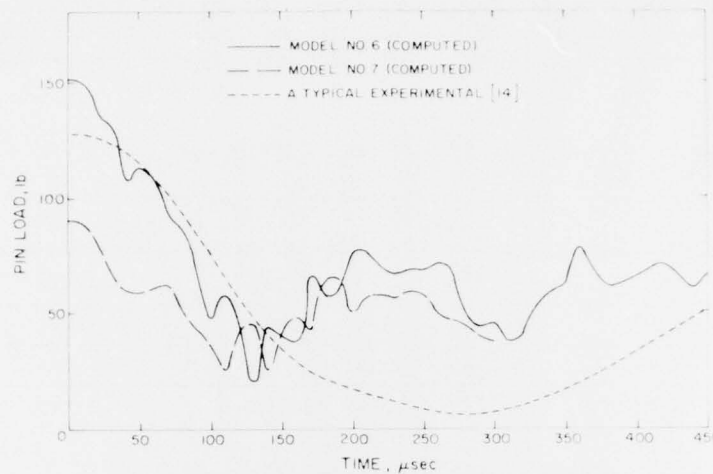
Fig. (9) - Pin load versus time in wedge-loaded C-DCB specimens

load cell system in the actual experimental setup.

DISCUSSION

An internal accuracy check of the dynamic finite element algorithm was made by computing the instantaneous energy balance of the entire system. Typical results for four crack lengths are shown in Tables 1 and 2. It is interesting to note that the accuracy of this energy balance is somewhat lower for Model No. 6 specimen which also showed larger oscillation in dynamic stress intensity factors with crack propagation.

CONCLUSIONS

A dynamic finite element algorithm has been developed for computing the dynamic stress intensity factors from experimentally determined crack position versus the relation of a propagating and arresting crack. Accuracy of the developed numerical procedure was checked by comparing the numerically determined stress intensity factors with those determined in four dynamic photoelastic experiments.

The numerically and experimentally determined dynamic stress intensity factors of two wedge-loaded DCB specimens indicate that the crack propagates under a fixed grip condition.

ACKNOWLEDGEMENT

The results of this investigation were obtained in a research contract

TABLE 1 - ENERGY BALANCE IN C-DCB MODEL NO. 6

Crack Extension	W	U	K	F	(U + K + F)/W - 1
1.0	3.201	2.221	0.223	0.534	- 0.070
2.0	3.201	1.956	0.074	0.879	- 0.091
3.0	3.201	1.748	0.038	1.114	- 0.094
3.5*	3.201	1.629	0.055	1.154	- 0.113

TABLE 2 - ENERGY BALANCE IN C-DCB MODEL NO. 7

Crack Extension	W	U	K	F	(U + K + F)/W - 1
0.25	1.084	0.957	0.015	0.079	- 0.033
0.50	1.084	0.867	0.034	0.116	- 0.067
0.75	1.084	0.855	0.015	0.155	- 0.059
0.875*	1.084	0.836	0.005	0.181	- 0.062

* Crack Arrest

W: External Work   Unit: Pound-in.
U: Strain Energy
K: Kinetic Energy
F: Fracture Energy $\equiv \int_o^c \mathcal{G}\, dc$
c: Length of Crack Extension

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REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER TR No. 28	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER TR-28
4. TITLE (and Subtitle) A Procedure for Evaluating Fracture Dynamic Parameters from Crack Velocity Measurements		5. TYPE OF REPORT & PERIOD COVERED Interim Report
		6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) A.S. Kobayashi and S. Mall		8. CONTRACT OR GRANT NUMBER(s) N00014-76-C-0060 NR 064-478
9. PERFORMING ORGANIZATION NAME AND ADDRESS University of Washington Department of Mechanical Engineering Seattle, Washington 98195		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
11. CONTROLLING OFFICE NAME AND ADDRESS Office of Naval Research Arlington, Virginia		12. REPORT DATE May 1977
		13. NUMBER OF PAGES 13
14. MONITORING AGENCY NAME & ADDRESS(if different from Controlling Office)		15. SECURITY CLASS. (of this report)
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE

16. DISTRIBUTION STATEMENT (of this Report)

Unlimited

17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)

18. SUPPLEMENTARY NOTES

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

Fracture Mechanics   Impact
Crack Propagation   Dynamic Photoelasticity
Crack Arrest

20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

A combined numerical and experimental procedure for evaluating some of the fracture dynamic parameters which govern the crack run-arrest response in a fracturing plate are discussed. A dynamic finite element code is used to compute the dynamic stress intensity factor and dynamic energy release rate associated with a propagating crack which is driven by the experimentally determined crack velocity. Numerical results generated by the developed procedure are then compared with dynamic stress intensity factors obtained through dynamic photoelastic analyses of fracturing Homalite-100 plates. Two (OVER)

DD FORM 1473 EDITION OF 1 NOV 65 IS OBSOLETE
1 JAN 73
S/N 0102-014-6601

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

ABSTRACT (Continued)

edge-cracked specimens with fixed edge displacement loadings and two wedge-loaded
double cantilever beam specimens were considered in this comparative study.
Good agreements were obtained between the results obtained by the developed
numerical-experimental procedure and dynamic photoelasticity.

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